

# Promoting Teaching Mathematics through Problem Solving Using Lesson Study

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National Institute for Science and Mathematics  
Education Development (UP NISMED)

# Coverage of the Presentation

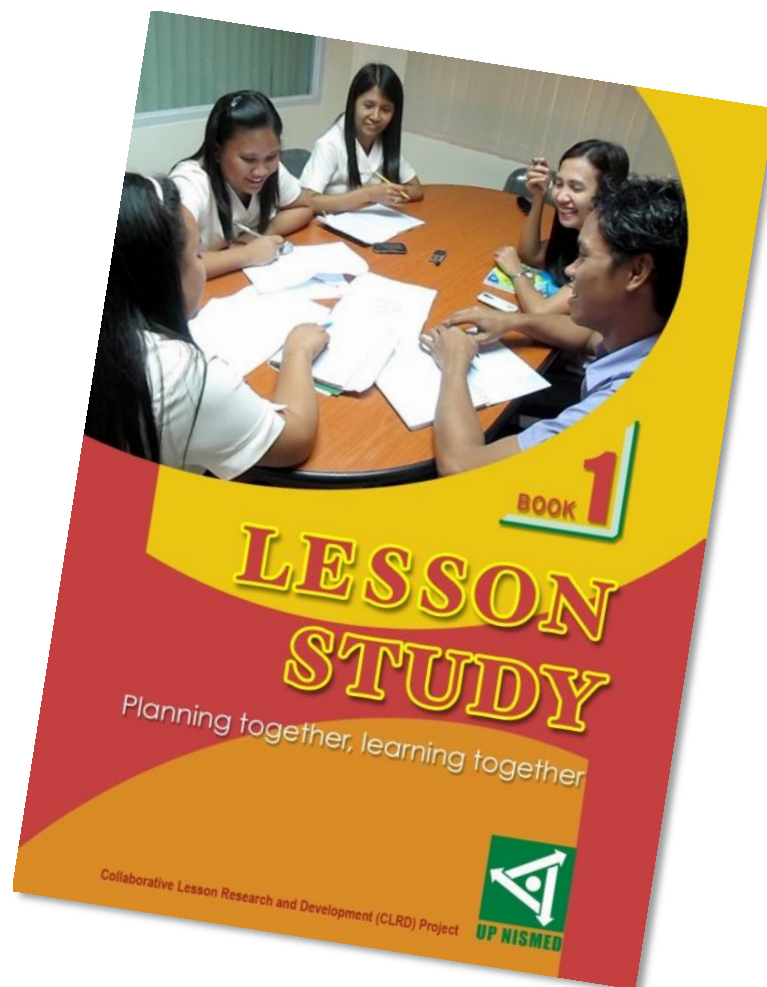
- UP NISMED's Lesson Study Project  
(Collaborative Lesson Research and Development Project)
  - Collaboration with teachers in schools
  - Lesson Study Book 1
  - Lesson Study Website
  - National Conference on Lesson Study
- Lesson Study on Typhoons and Floods

# The Collaborative Lesson Research and Development Project

- Covers the three main functions of NISMED
  - research
  - curriculum development
  - professional development of teachers
- Involves all academic staff of NISMED
  - Elementary School Mathematics
  - High School Mathematics
  - Elementary School Science
  - High School Earth and Environmental Science
  - High School Biology
  - High School Chemistry
  - High School Physics
  - (Audiovisual Group)

# The Collaborative Lesson Research and Development Project

- Uses lesson study to promote teaching:
  - mathematics through problem solving
  - science through inquiry
- Includes all mathematics and science subjects in grades 1 to 10 of basic education
- Involves collaboration with teachers from 7 schools



## Contents

### Preface

### Introduction

|                                                 |  |
|-------------------------------------------------|--|
| NISMED's Journey in Adapting Lesson Study ..... |  |
| Implementing the Lesson Study Process .....     |  |

### NISMED's Initial Experience

|                                                                                     |  |
|-------------------------------------------------------------------------------------|--|
| Improving Teacher Effectiveness in High School Chemistry through Lesson Study ..... |  |
|-------------------------------------------------------------------------------------|--|

### I. Treading the Uncharted Waters of Lesson Study .....

|                                                                                                                   |  |
|-------------------------------------------------------------------------------------------------------------------|--|
| Introducing Collaborative Lesson Planning to Elementary School Science Teachers: Challenges and Constraints ..... |  |
|-------------------------------------------------------------------------------------------------------------------|--|

|                                                                                                        |  |
|--------------------------------------------------------------------------------------------------------|--|
| Growing up Pains: Reflections of Five Chemistry Teachers on the First Two Cycles of Lesson Study ..... |  |
|--------------------------------------------------------------------------------------------------------|--|

|                                                                                |  |
|--------------------------------------------------------------------------------|--|
| Fostering Collaboration in Collaborative Lesson Research and Development ..... |  |
|--------------------------------------------------------------------------------|--|

### II. Taking on New Roles in Teaching and Learning through Lesson Study .....

|                                                                            |  |
|----------------------------------------------------------------------------|--|
| Developing Problem Solving Abilities through Multiple-Solution Tasks ..... |  |
|----------------------------------------------------------------------------|--|

|                                                                           |  |
|---------------------------------------------------------------------------|--|
| An Analysis of a Problem Solving Activity in a Mathematics II Class ..... |  |
|---------------------------------------------------------------------------|--|

### III. Empowering Students to Think, Communicate and Learn through Lesson Study.....

|                                                                                  |  |
|----------------------------------------------------------------------------------|--|
| Teaching through Problem Solving: Assessing Students' Mathematical Thinking..... |  |
|----------------------------------------------------------------------------------|--|

|                                                                |  |
|----------------------------------------------------------------|--|
| Probing into Students' Learning Processes through Interview .. |  |
|----------------------------------------------------------------|--|

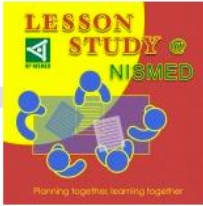
|                                                                                                                      |  |
|----------------------------------------------------------------------------------------------------------------------|--|
| Using Students' Preferred Language to Engage Them Actively in Learning About How Fast Solids Dissolve in Water ..... |  |
|----------------------------------------------------------------------------------------------------------------------|--|

### IV. Initiating and Sustaining Collaboration Among Teachers .....

|                                                                                                   |  |
|---------------------------------------------------------------------------------------------------|--|
| Reflecting on Classroom Problem Solving Practices Involving Multiplication of Whole Numbers ..... |  |
|---------------------------------------------------------------------------------------------------|--|

|                                                         |  |
|---------------------------------------------------------|--|
| Scaffolding Teacher Learning through Lesson Study ..... |  |
|---------------------------------------------------------|--|

|                                                                      |  |
|----------------------------------------------------------------------|--|
| Beyond Collaboration: An Appreciative Inquiry Into Lesson Study..... |  |
|----------------------------------------------------------------------|--|



LESSON STUDY @UP NISMED

Planning together, learning together

- Home
- About
- What is lesson study?
- UP NISMED
- AglMat
- GeoGebra
- KaSaMa

## Lesson Study @UP NISMED

Planning together, learning together



### NISMED Introduces Lesson Study to PMA

A seminar-workshop for Mathematics teachers of the Philippine Military Academy was conducted on March 6-8, 2012. Held at PMA, Fort del Pilar, Baguio City, this was attended by 23 participants ...

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### NISMED spearheads Lesson Study in the Philippines

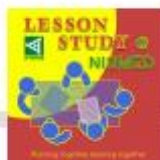
Lesson study is a teacher-led professional development model where a group of classroom teachers works collaboratively to plan and design a lesson and study student learning by systematic inquiry. In ...

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Dedicated for the promotion of Lesson Study in the Philippines

*Lesson study* is a school-based , teacher-led continuing professional development model where a group of classroom teachers work collaboratively to plan, design, implement, and improve a lesson and study student learning and thinking by systematic inquiry.



Home  
About  
What is lesson study?  
UP NISMED  
Ag/Mat  
Geo/Chem  
Ka/Ala

### Uncovering Alternative Conceptions of Diffusion and Osmosis Through Lesson Study

Through lesson study, a research lesson on diffusion and osmosis was developed collaboratively among four Biology teachers of a partner high school in Metro Manila and four NISMED researchers. The group developed a structured inquiry activity on diffusion and osmosis using existing activity sheets of the partner teachers as reference. Student learning and alternative conceptions were closely observed during the implementation of the lesson.



Students performing the experiment

Through classroom observations, analysis of accomplished activity sheets, and student interviews, it was revealed that students have difficulties in differentiating diffusion from osmosis, and understanding the terms hypertonic, hypotonic, and isotonic. Students also perceived that there is a directed movement of particles from a higher concentration to a lower concentration. This suggests their inability to integrate random molecular motion and collisions in explaining the movement of molecules. Identification of these alternative conceptions is an important prerequisite to developing appropriate lessons and activities. Appropriate computer animations may be used in conjunction with other instructional strategies to scaffold students' understanding and visualization of random molecular motion and collisions to better understand diffusion and osmosis. To improve the research lesson and address the misconceptions identified, the next step would be going through another cycle: revisiting, revising, and implementing the research lesson.

The full text of the study is one of the chapters of the book titled "BOOK 1. LESSON STUDY: PLANNING TOGETHER, LEARNING TOGETHER" which will be published in print form by UP NISMED this first quarter of 2013.

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#### Information

This entry was posted on January 4, 2013 by Miki de Hita-Catalan in Science and tagged alternative conceptions, diffusion, lesson study.

#### Shortlink

<http://wp.me/p22Dp1-4K>

#### Navigation

[Previous post](#)  
[Next post](#)



#### Top Posts & Pages

UP NISMED's Initial Experience with Lesson Study: Improving Teacher Effectiveness in High School Chemistry  
Beyond Collaboration: An Appreciative Inquiry into Lesson Study  
Growing up Pains: Reflections of Five Chemistry Teachers on the First Two Cycles of Lesson Study  
Uncovering Alternative Conceptions of Diffusion and Osmosis Through Lesson Study  
Classroom Problem Solving Practices Involving Multiplication of Whole Numbers  
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# National Conference in Science and Mathematics Education 2013

**Theme:** *Empowering Teachers for the K to 12 Curriculum through Lesson Study*

<http://ncsme2013.nismmed.upd.edu.ph/>

The screenshot shows the homepage of the National Conference in Science and Mathematics Education 2013 website. The header features the conference title, theme, dates (22-24 October 2013), and location (UP NISMED, Diliman, Quezon City). A navigation menu includes links for HOME, CALL FOR CONTRIBUTIONS, REGISTRATION, PROGRAM OF ACTIVITIES, ACCOMMODATION, MEMO/ADVISORY, and ABOUT LESSON STUDY. A large banner image depicts a group of teachers in a lesson study session. Below the banner, a text block describes the conference's purpose and objectives. The objectives are listed as follows:

1. Promote lesson study as a professional development model to enhance the capability of teachers in implementing the K to 12 Curriculum (Mathematics and Science);
2. Promote teaching of science through inquiry and teaching of mathematics through problem solving in lesson study;
3. Provide a forum for sharing of experiences and research results related to lesson study; and,
4. Initiate a local network on lesson study.

Below the objectives, a text block states: "To achieve these objectives, there will be plenary and parallel sharing of research results and practices, demonstration teaching, discussion groups, and poster presentations." At the bottom left, there is a "Recommend this on Google" button and a "Subscribe to: Posts (Atom)" link. On the right side, there is a "KEEP IN TOUCH" section with social media icons for Twitter, Facebook, and Email. Below that is a "LIKE US ON FACEBOOK" section with a Facebook Like button and a photo gallery of participants. At the bottom right, there is a "REGISTRATION FORM" link.

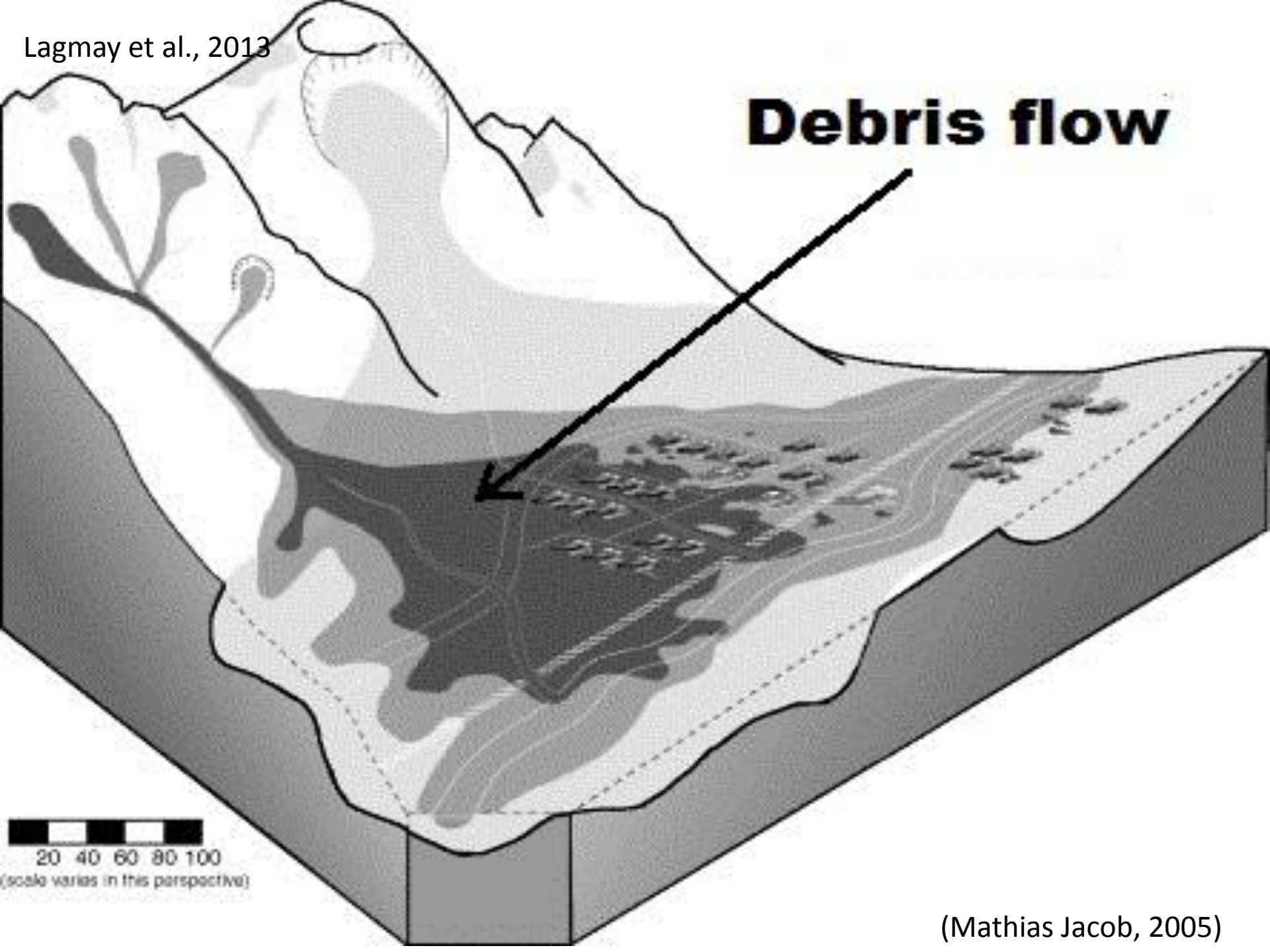
# Objectives of NCSME 2013

- To promote lesson study as a professional development model to enhance the capability of teachers in implementing the K to 12 curriculum in mathematics and science
- To promote the teaching of science through inquiry and the teaching of mathematics through problem solving in lesson study
- To provide a forum for sharing experiences and research results related to lesson study
- To initiate a local network on lesson study

# Lesson Study on Floods and Typhoons

Lagmay et al., 2013

# Debris flow



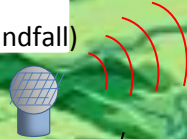
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(scale varies in this perspective)

(Mathias Jacob, 2005)



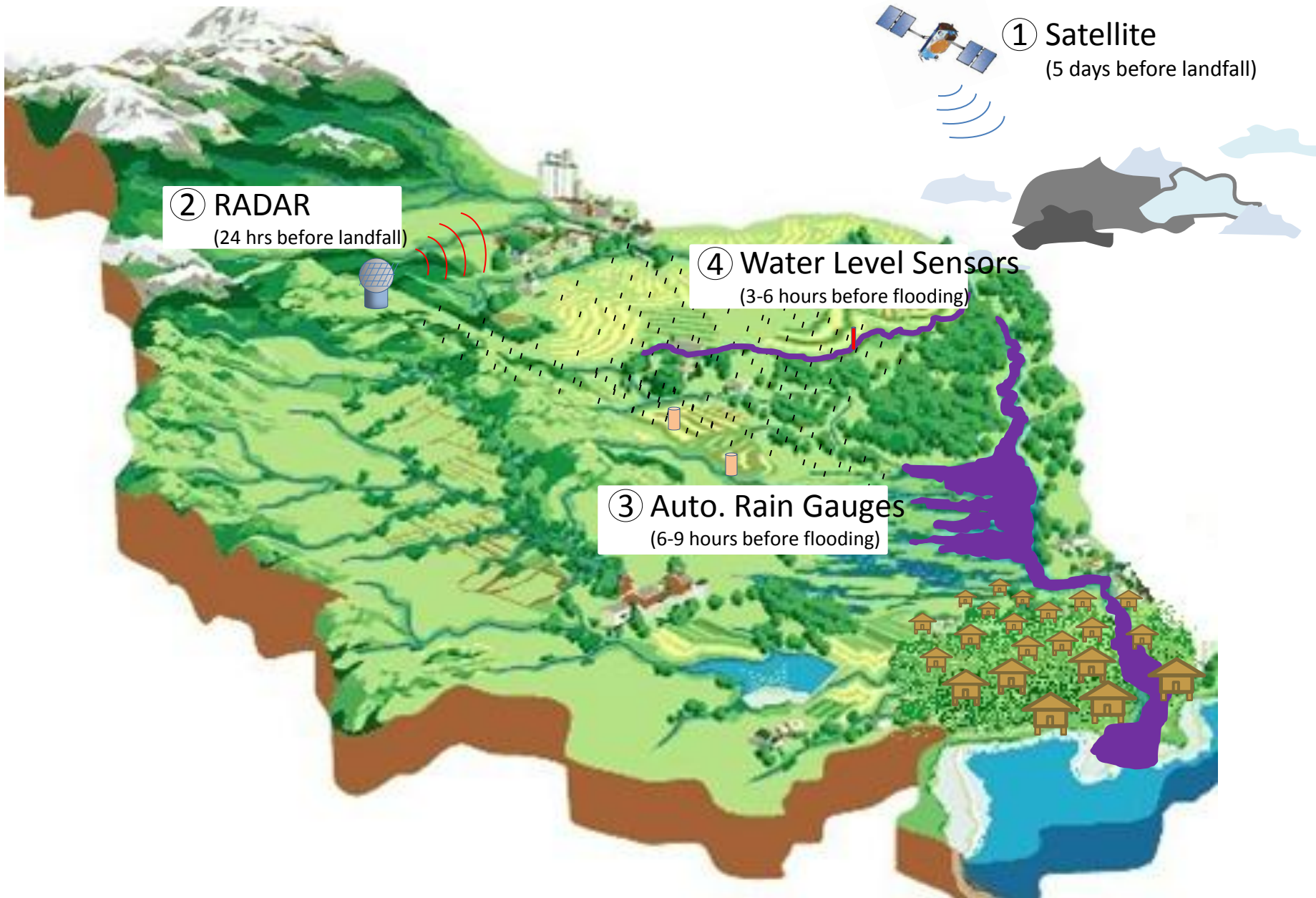
① Satellite  
(5 days before landfall)

② RADAR  
(24 hrs before landfall)



④ Water Level Sensors  
(3-6 hours before flooding)

③ Auto. Rain Gauges  
(6-9 hours before flooding)



# Mathematical Tasks (in Tokyo Meeting)

## Estimating Area and Volume

Task 1:

Concept: Area of irregular shapes

Skill: Estimating the area of an irregular shape in different ways

Task 2:

Concept: Ratio

Skill: Interpreting scales on maps

Task 3:

Concept: Volume

Skill: Reading a rain gauge and interpreting what mm of rain means

Task 4:

Concept: Volume

Skill: Calculating the height of the flood, given the area of the lowland



Long-term goal: To develop students' mathematical thinking through problem solving

Sub-goals:

1. To represent real-life and mathematical situations
2. To give meaning to those representations
3. To solve problems in different ways

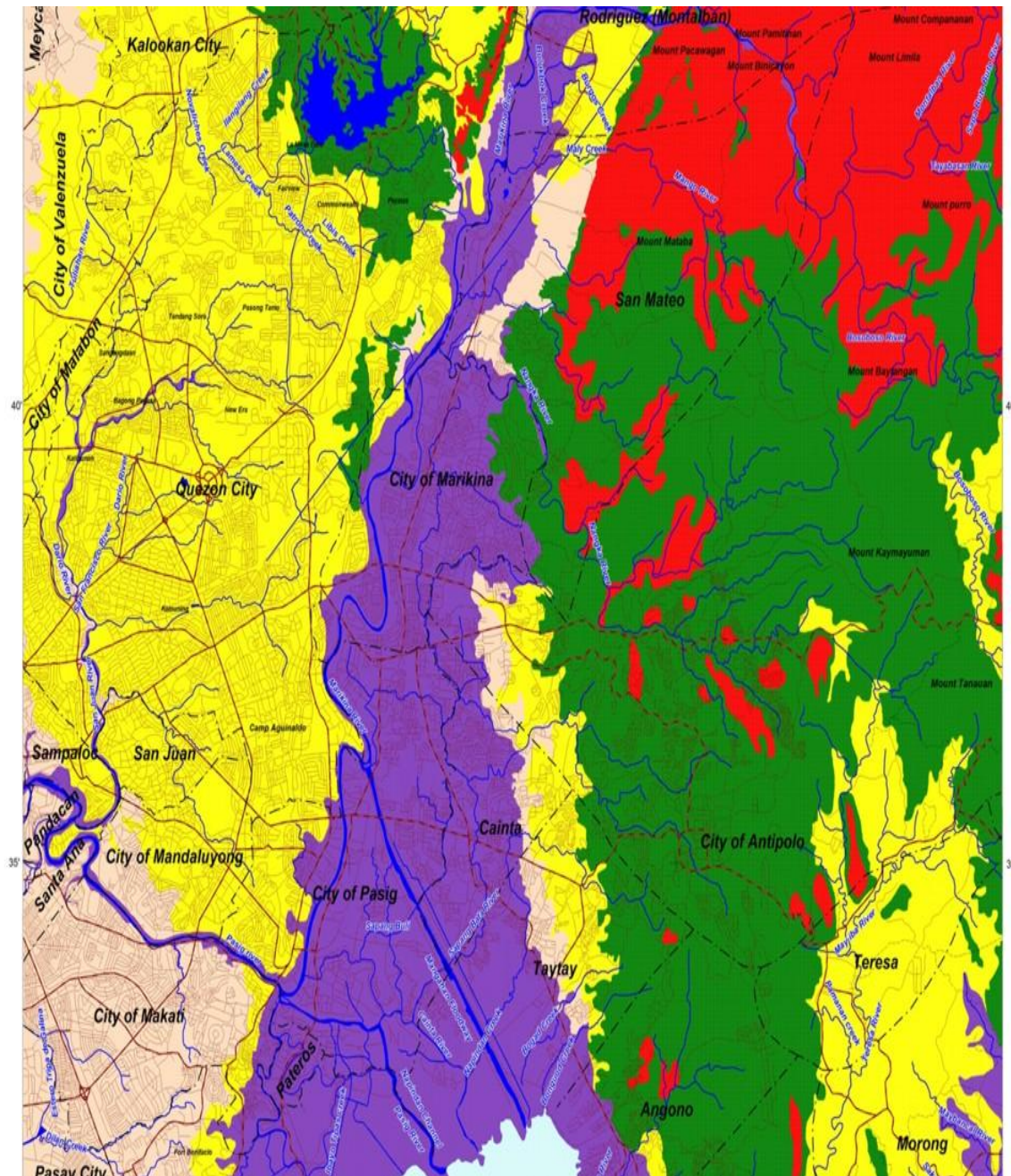
# Our “Collaborators” at Sta. Lucia High School

- Principal
- Mathematics department head
- 4 Grade 7 mathematics teachers

**PLANNING**







#### LEGEND :

- **High susceptibility to landslide**  
Areas with high landslide susceptibility rating have active/recent landslides and tension cracks that would directly affect the community. Those with steep slopes and drainages that are prone to landslide damming are also highly susceptible to landslides.
- **Moderate susceptibility to landslide**  
Areas with moderate landslide susceptibility rating have inactive/recent landslides and tension cracks which are located away from the community. These areas usually have moderate slopes.
- **Low susceptibility to landslide**  
Areas with low to gentle slopes and lacking tension cracks have low landslide susceptibility rating.
- **High susceptibility to flooding**  
Areas with greater than 1 meter flood height. These areas are usually flooded for several hours during heavy rains, include landforms of topographic lows such as active river channels, abandoned river channels and areas along river banks; also prone to flashfloods.
- **Low to moderate susceptibility to flooding**  
Areas with less than 1.0 meter flood height. These are usually inundated during prolonged and extensive heavy rainfall or extreme weather condition.

- Main road
- Secondary road
- Trail road
- River
- Municipal boundary

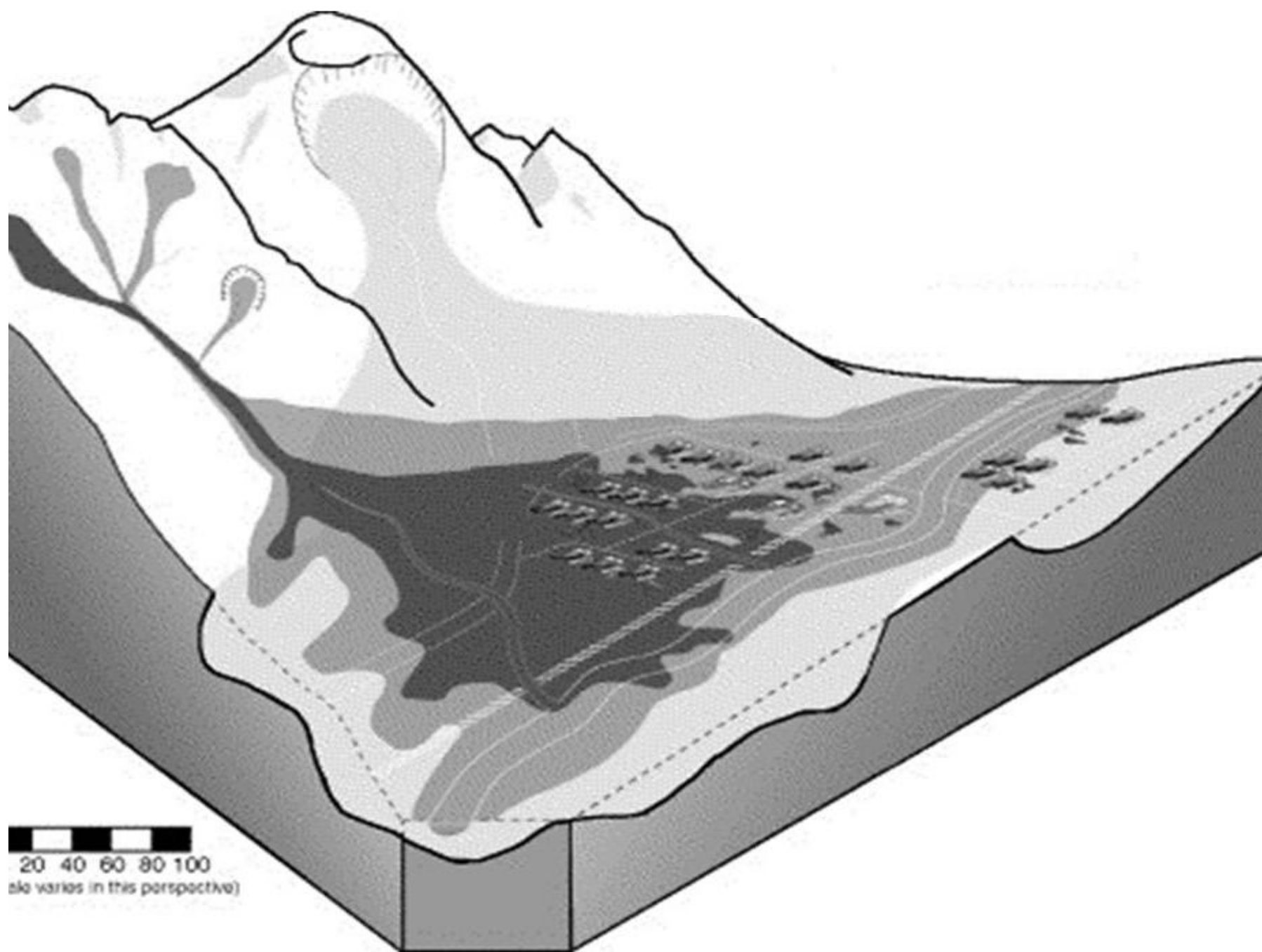


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kilometers

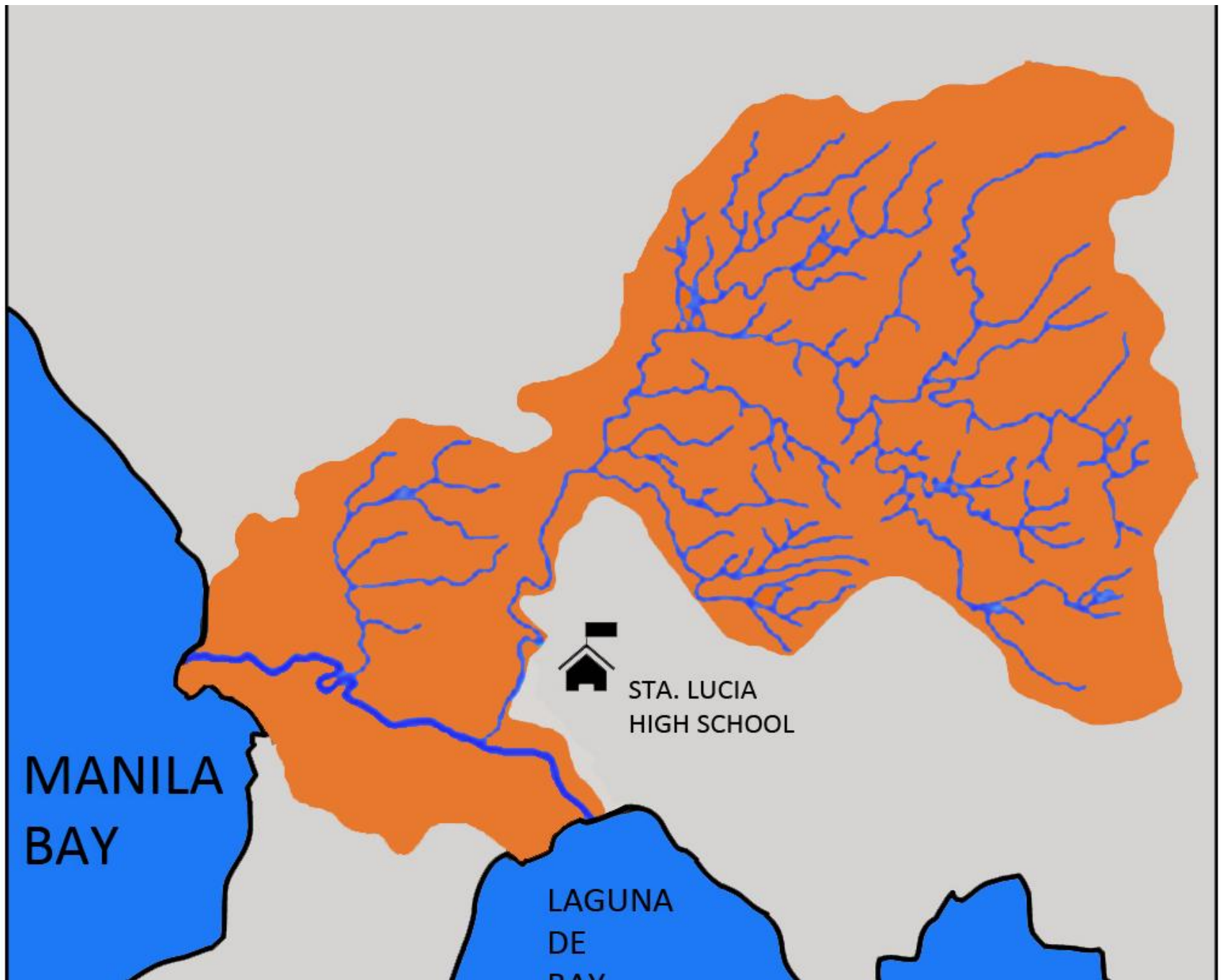
TRANSVERSE MERCATOR PROJECTION  
MAPPING SCALE 1:50,000

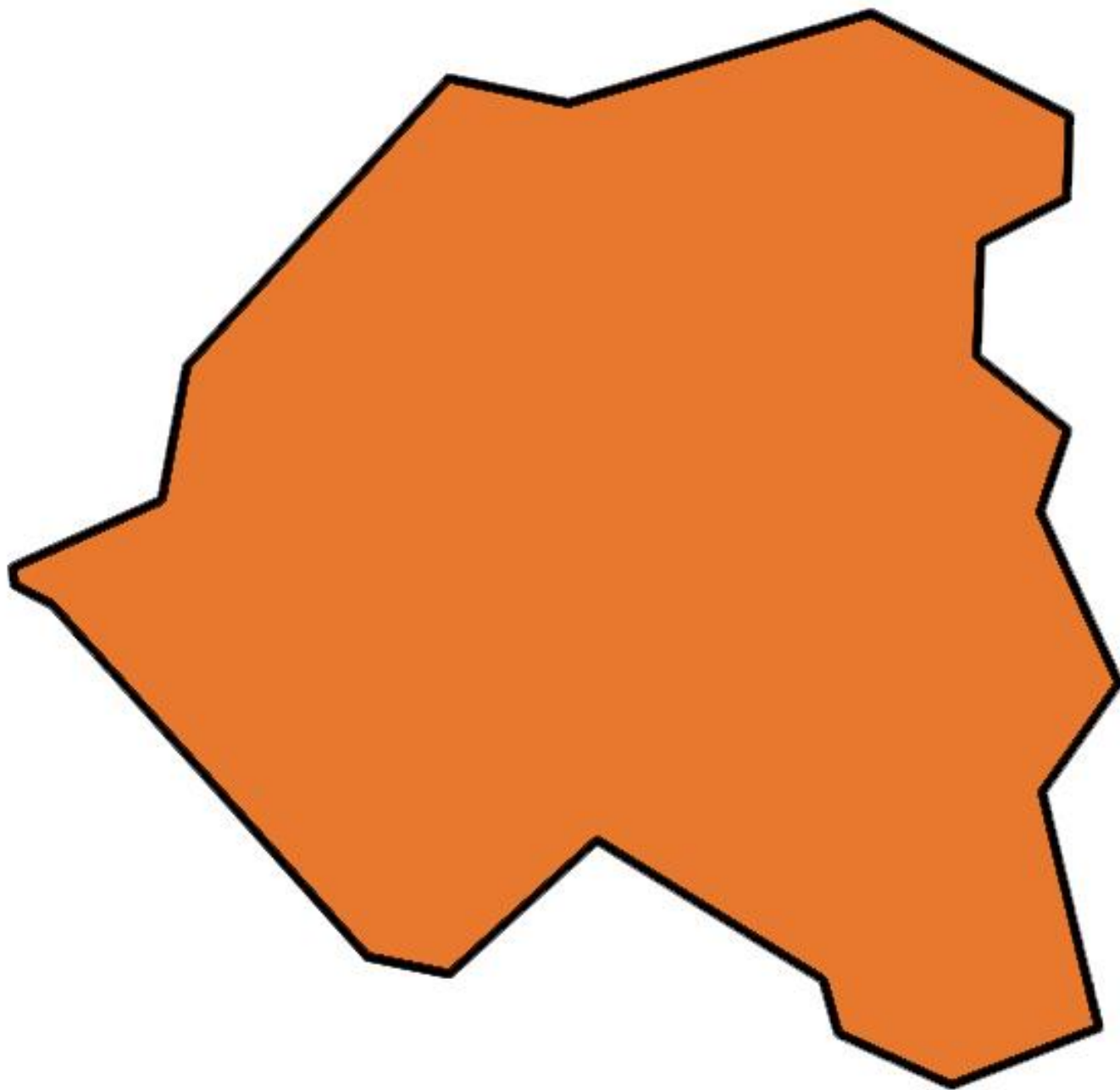
GIS Processing :  
Lands Geological Survey Division

Data Sources:  
MGB Geohazard Assessment Team  
Geological Database and Information Systems Section  
Lands Geological Survey Division  
Data collected from MGB PIA



also varies in this perspective)





# MATHEMATICS VII

**SEPTEMBER 9, 2010**

**SUBJECT MATTER:** Area of an Irregular Shape

**OBJECTIVES:**

- Find the area of an irregular shape
- Determine the volume of an irregular shape
- Appreciate the application of determining areas and volumes

**PROCEDURE**

**MOTIVATION**

- Video presentation of typhoon Ondoy.

***Enabling Questions***

- » Do you remember typhoon Ondoy?
- » What have you experienced during the typhoon?
- » What caused the flood?
- » Where do you think the water came from that caused massive flooding in Pasig and Marikina?

**PRESENTATION**

- Discussion of watershed.
- Distribution of activity sheet.
  - Think of different ways on how will you measure the area of watershed of Pasig and Marikina?
  - Find the area of this watershed using ruler.

**Scale: 1cm = 5km**

- Presentation of their activity
- Give the approximate measurement of watershed.
  - If the amount of water in a rain gauge is 1cm, what do you think is the volume of water in watershed that will cause flood in Pasig and Marikina?
  - Which is better the smaller area of watershed or the bigger area of watershed?

• **GENERALIZATION**

- What have you learned today?
- What is the importance of finding area?

# Highlights of the Planning

- The teachers said that it was their first time to find the area of an irregular shape.
- The teachers used two ways to find the area of the irregular shape: 1) embedding it with shapes that are familiar which they know how to get the area of 2) drawing grid lines to cover the irregular shape and counting the unit squares that cover the shape
- The lesson study group hoped that the students will be able to think of these ways and of other ways as well.
- The teachers decided that they will take up the tasks with their students depending on how the lesson will go.
- The teachers decided that they will show a video of flood during tropical storm Ondoy in September 2009 rather than show pictures of floods.
- They will show a model of a watershed and “simulate” rain using a spray.
- They will discuss disaster awareness at the start of the lesson and disaster preparedness at the end of the lesson.

# IMPLEMENTING THE RESEARCH LESSON

9 September 2013

8:20 – 9:20 am Section 2 (Ms. Eflida P. Tesorio)

10:20 – 11:20 am Section 14 (Ms. Anabelle N. Fuentes)

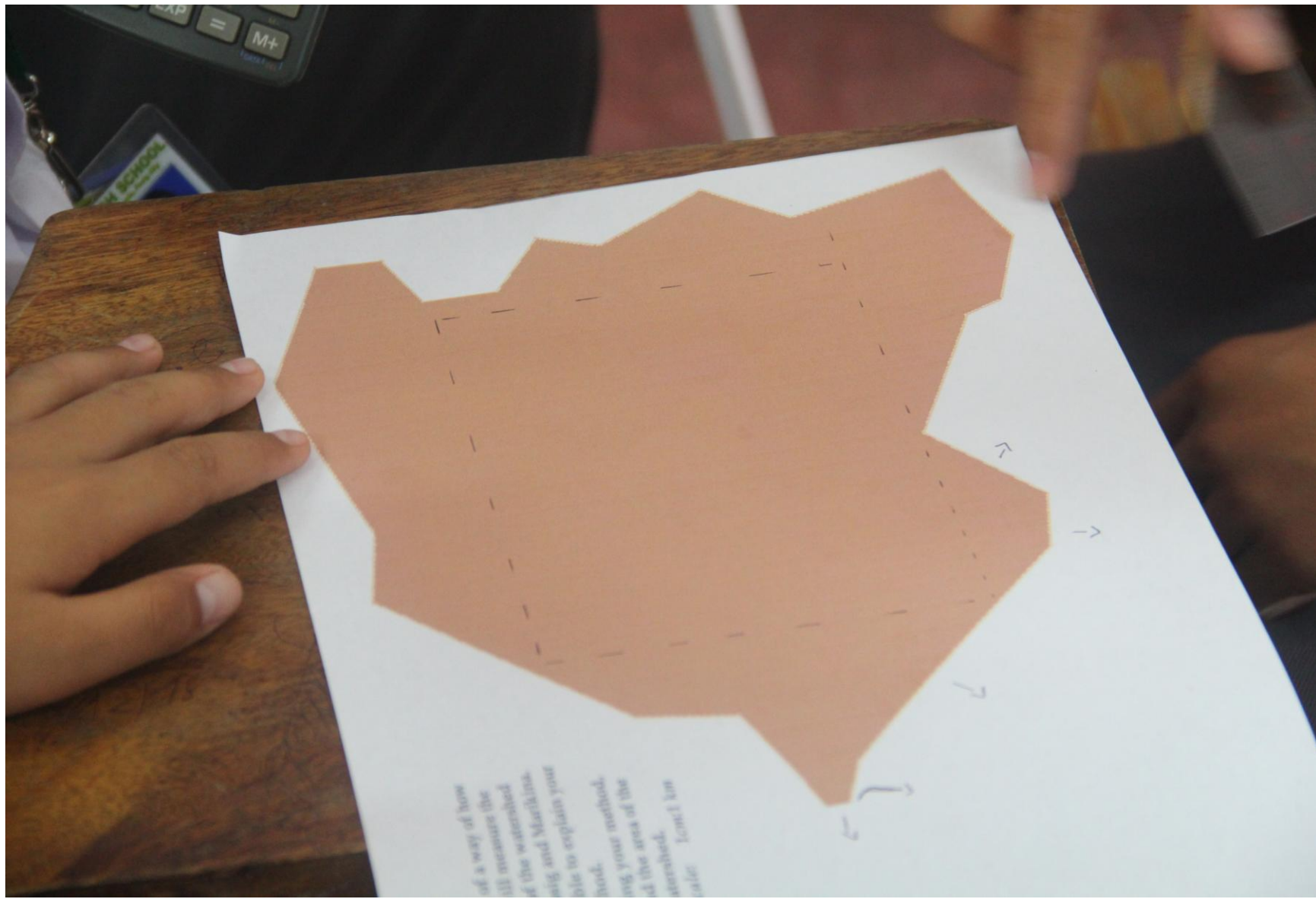
11:45 – 12:45 am Section 10 (Ms. Mia Paula G. Mosanto)

12:45 – 1:45 am Section 17 (Ms. Diana P. Sta. Rosa)

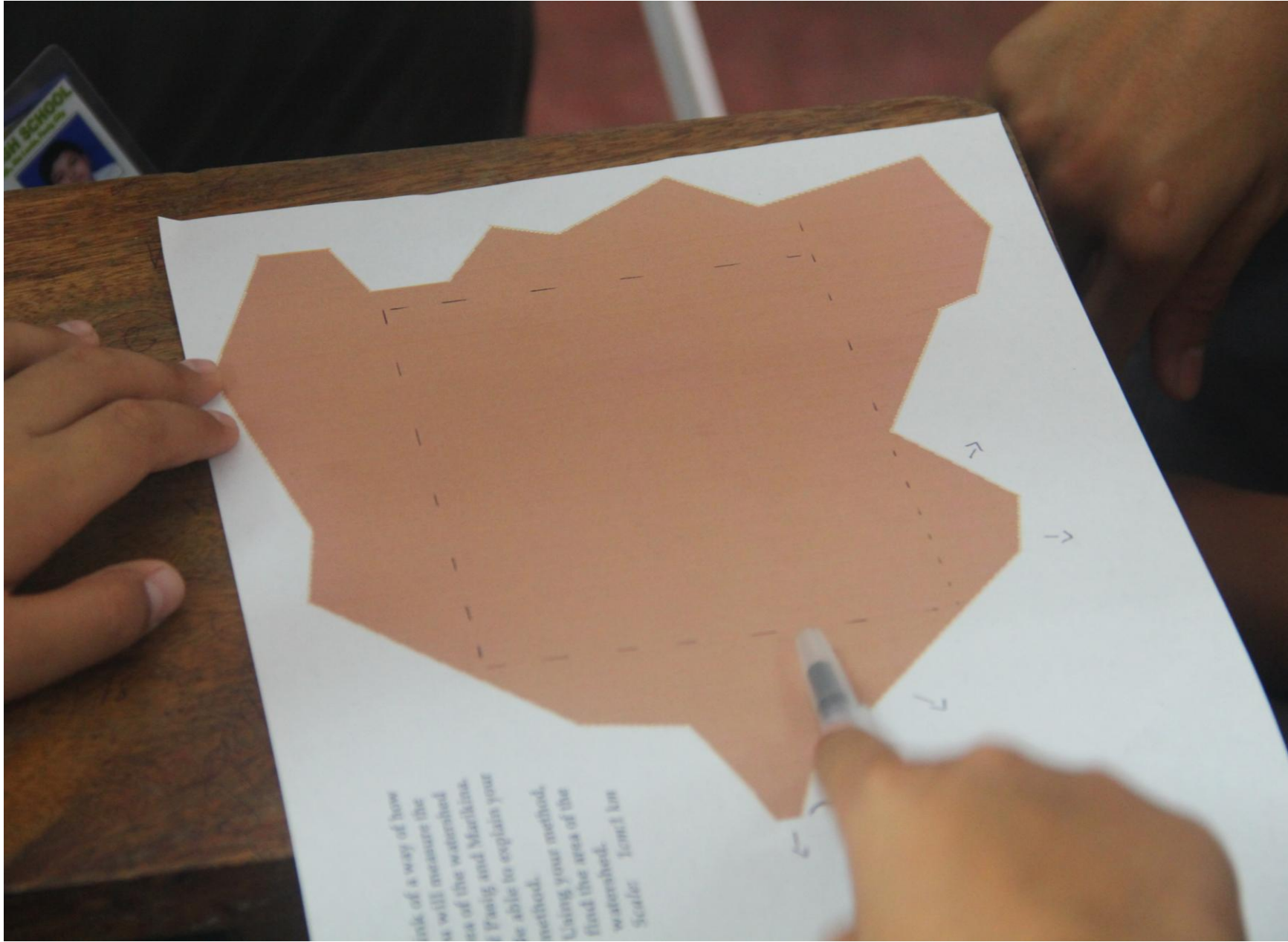
# First Implementation



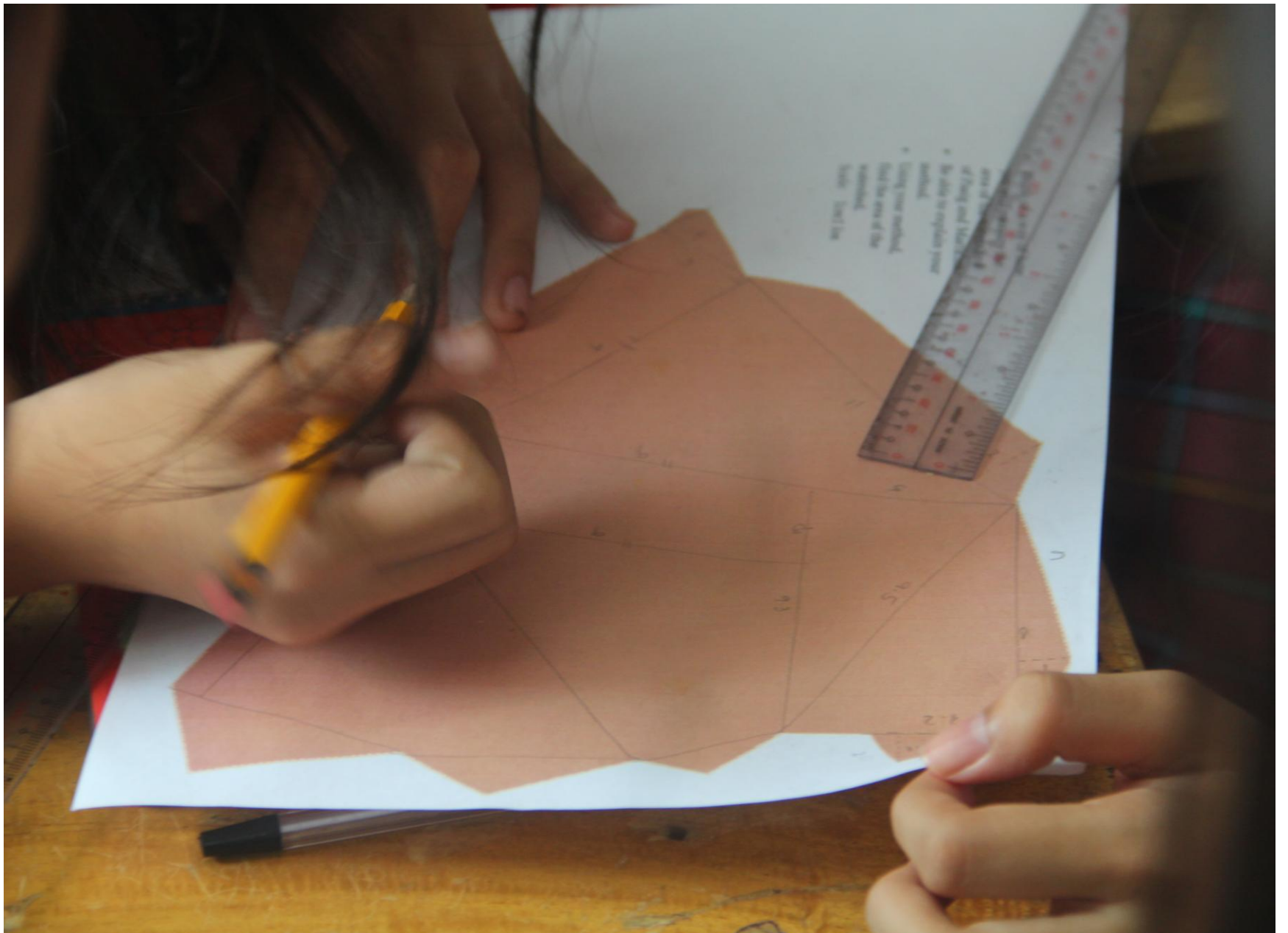




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head.  
ing your method.  
of the area of the  
determined.  
scale: 1cm:1 km

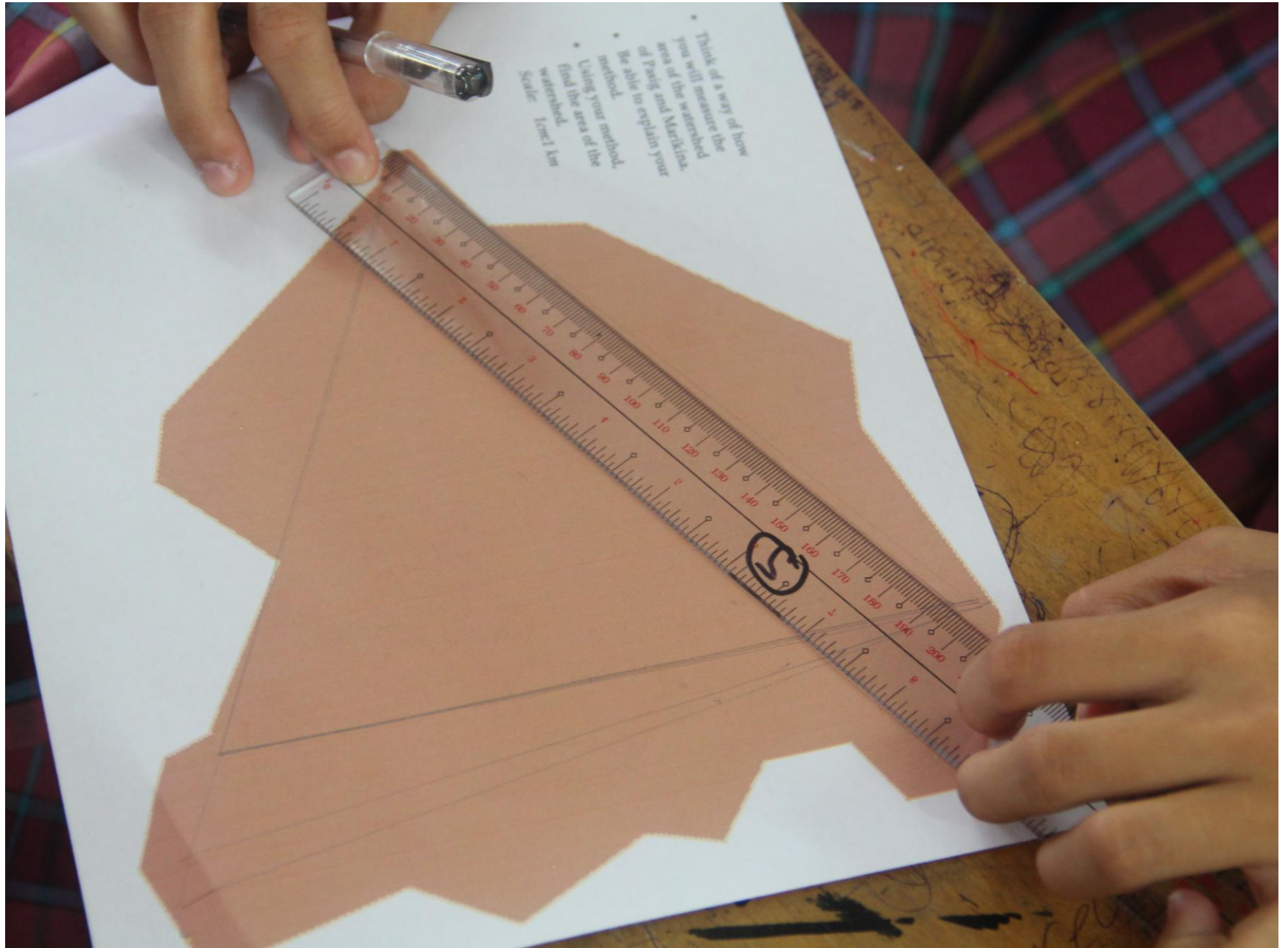


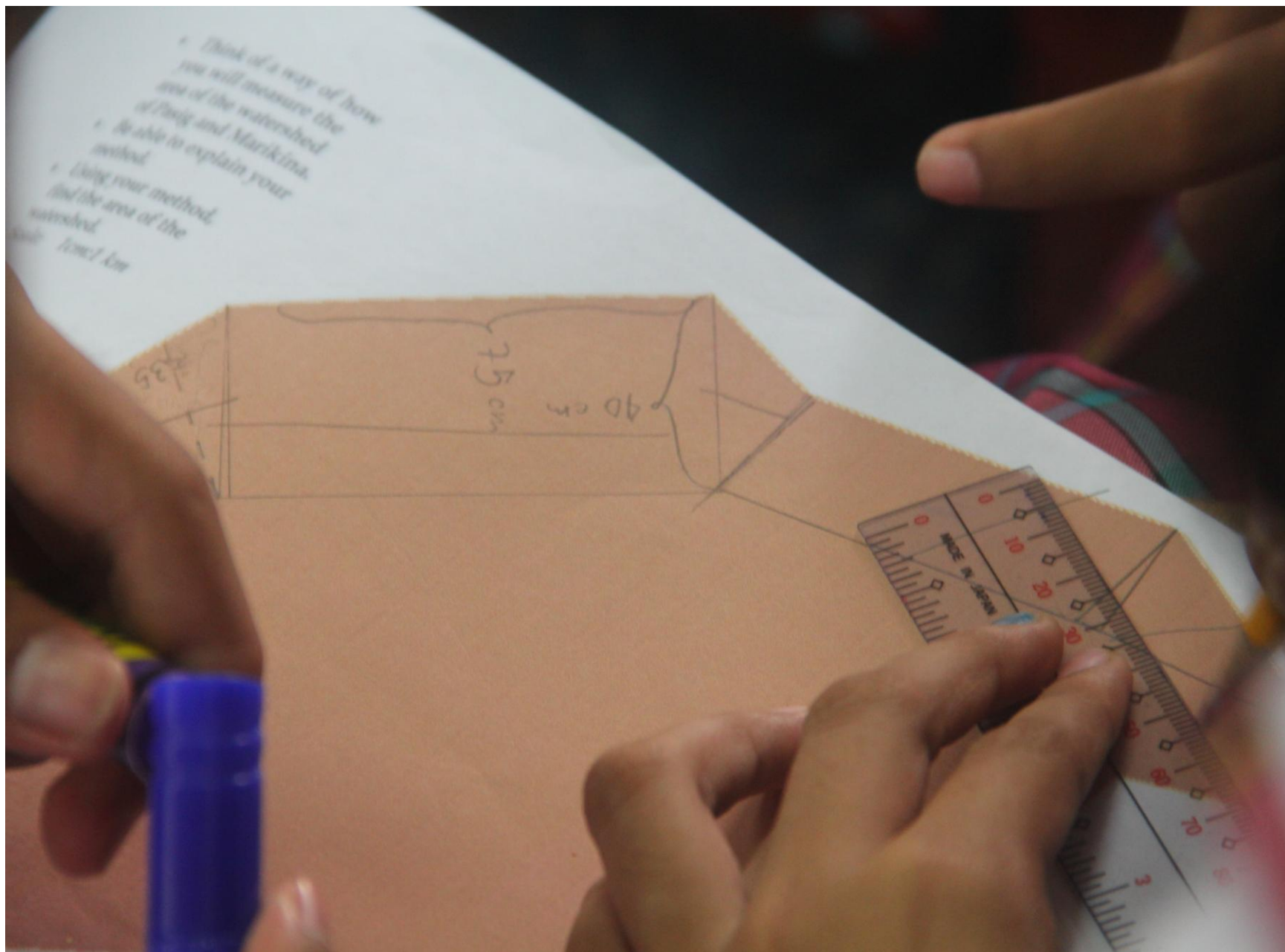
Scale of a way of how  
it will measure the  
area of the watershed.  
Using your method,  
find the area of the  
watershed.  
Scale: 1cm:1 km

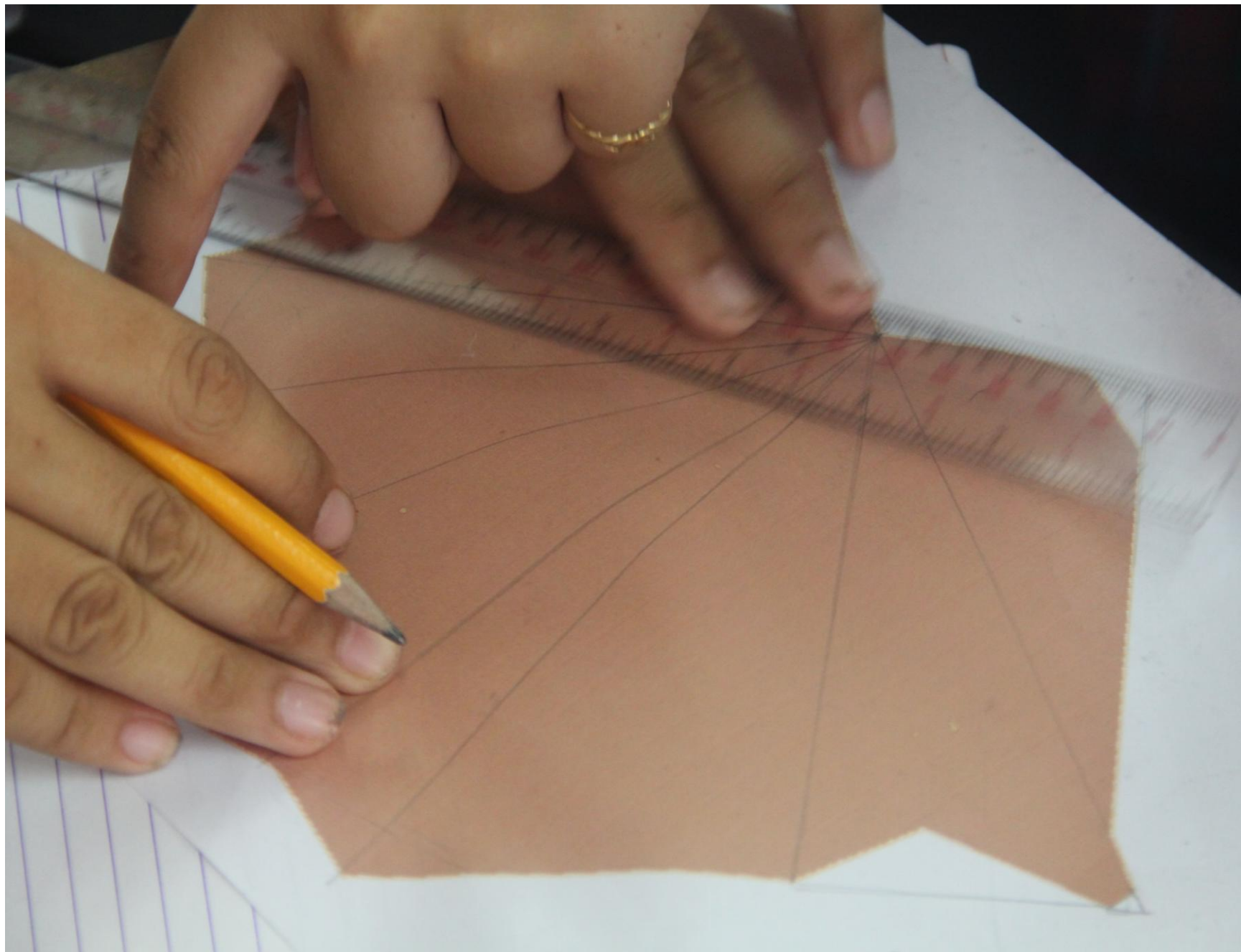




- Think of a way of how you will measure the area of the watershed of Pavia and Merikina.
  - Be able to explain your method.
  - Using your method, find the area of the watershed.
- Scale: 1cm:1 km









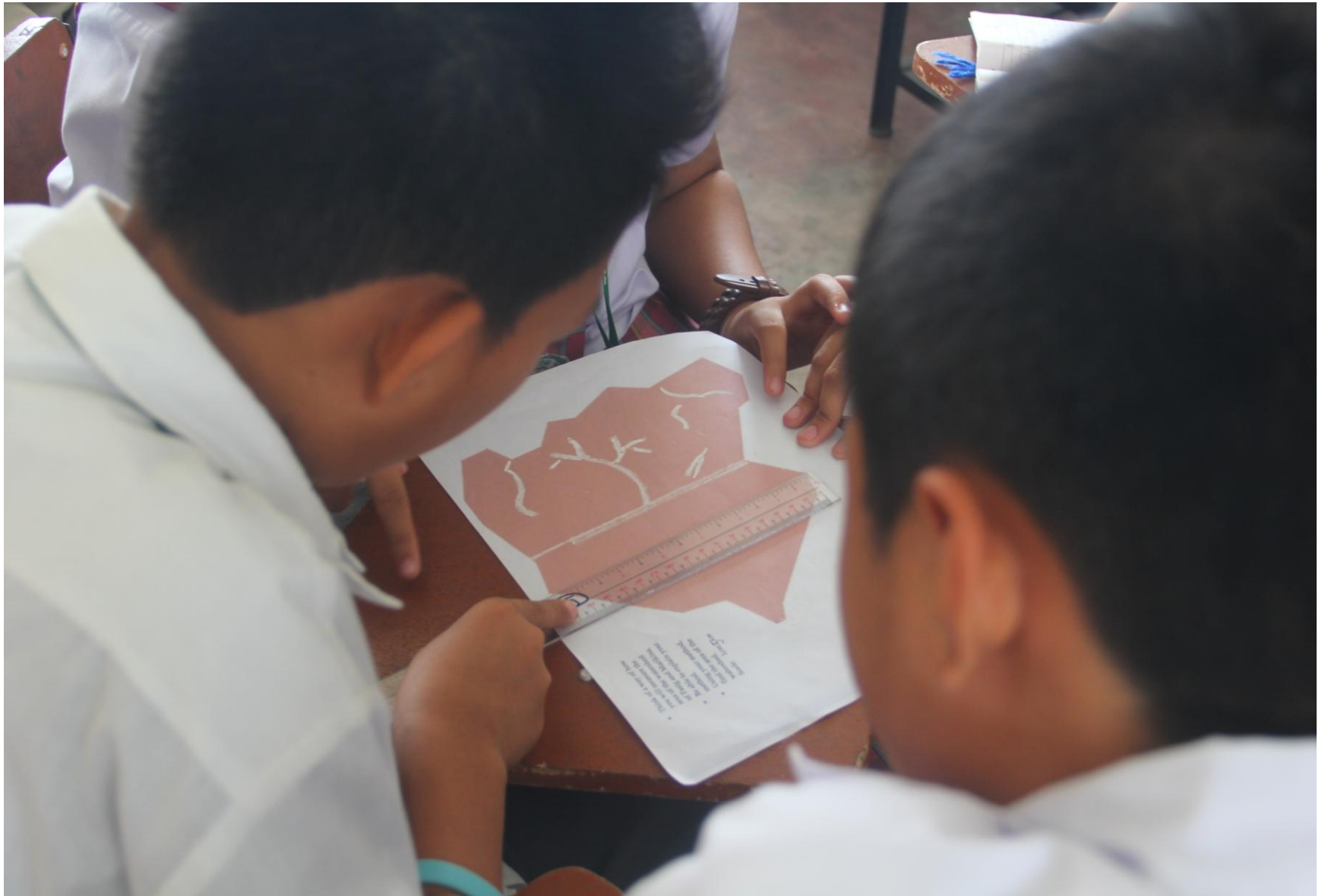


# Highlights of the Post-lesson Discussion

- Ask students to use fine pentel pen or chalk.
- Give time limit for the activity so that students will think first of a method that will enable them to get the area in a short time.
- Explain to the students that they are to measure the area of the watershed and not the area of the lowland.
- Ask why it is important for them to know the area of the watershed.

# Second Implementation



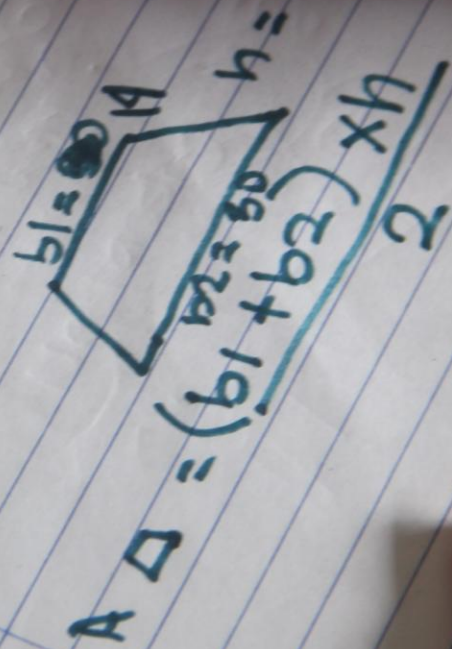






$$= \frac{(b_1 + b_2) \times h}{2}$$





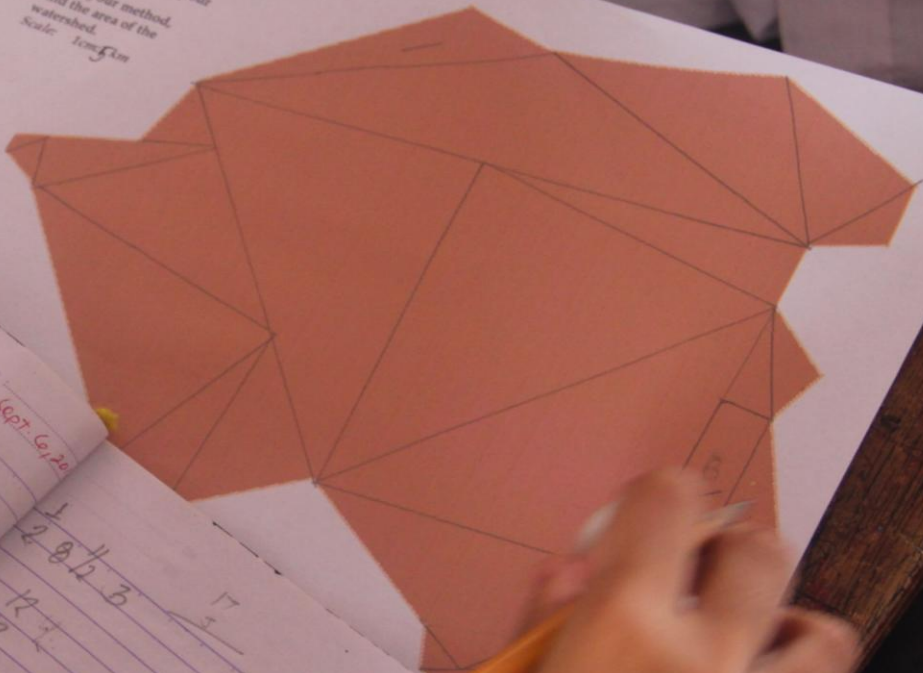
$$A \Delta = \frac{(b_1 + b_2) \times h}{2}$$







- Think of a way of how you will measure the area of the watershed of Pasig and Marikina.
  - Be able to explain your method.
  - Using your method, find the area of the watershed.
- Scale: 1 cm = 5 km



Area

- is the region enclosed by a plane figure. The unit of an area is the square of the unit like  $\text{cm}^2$ ,  $\text{ft}^2$ ,  $\text{m}^2$  and  $\text{km}^2$ .

Rectangle

$A = lw$



Square

$A = s^2$



Circle

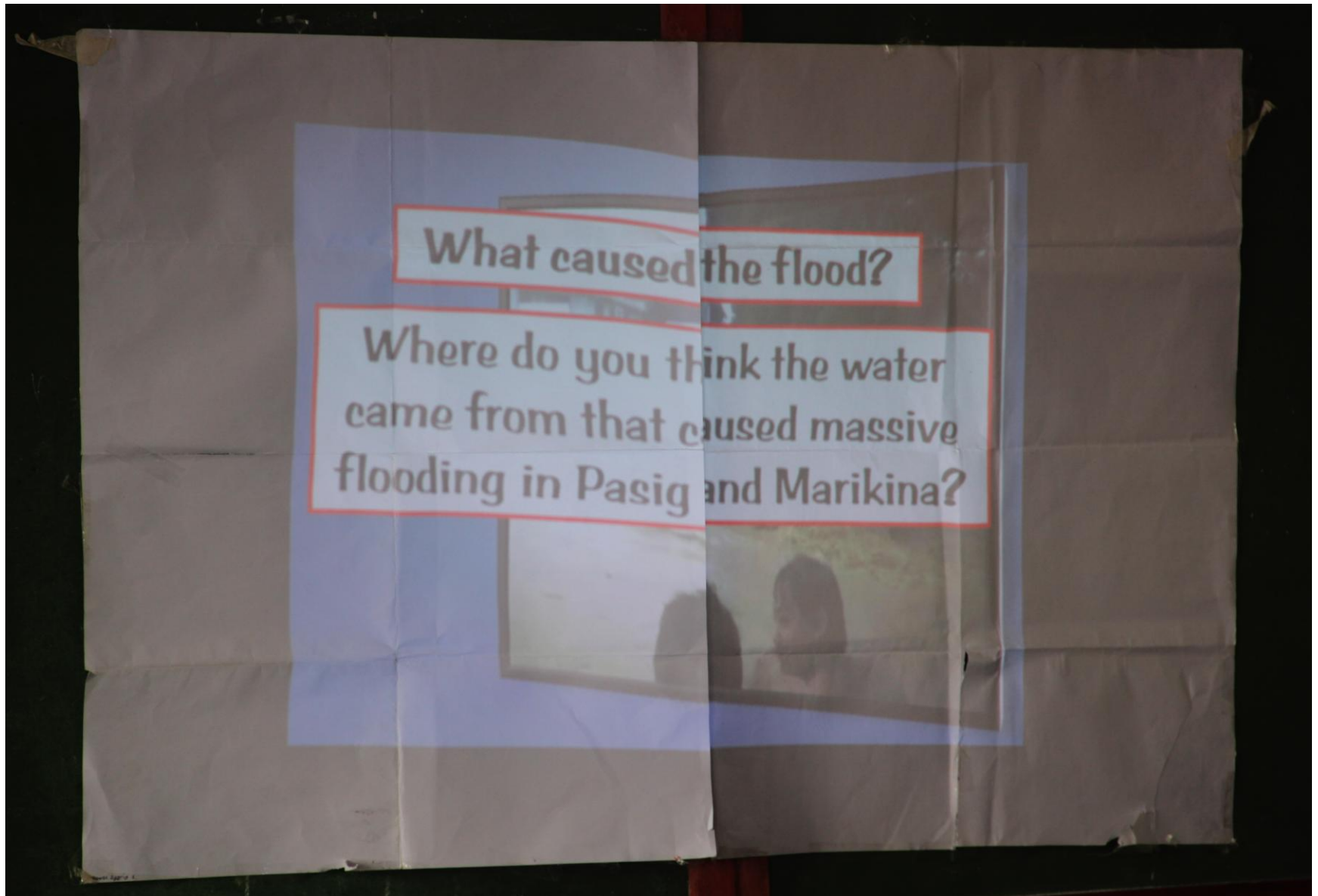
$A = \pi r^2$



Sept. 20

1  
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12 1  
12

# Fourth Implementation







# Students' ideas on how to prepare for typhoons and floods

- Always listen to the radio for weather and situation updates.
- Move to a higher place.
- Secure important documents.

# Highlights of the Post-lesson Discussion

- Discuss again with the students
  - how to use and read the ruler
  - how to use the formulas of the area of familiar shapes
  - difference between perimeter and area
- Ask students to summarize the methods of finding the area of an irregular shape (partitioning, use of grid, enclosing the shape with a familiar shape), compare them and determine which is better/best and why
- Show a picture of the watershed and lowland and emphasize that the area of the watershed and not the lowland was being determined.
- Process incorrect responses of students and “push students to the limits of their understanding.”

Thank you!